Linear and Non-Linear Responses to Dynamic Broad-Band Spectra in Primary Auditory Cortex

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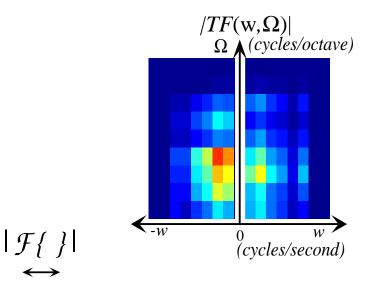
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By Way of Introduction

Cells in AI are well characterized their spectro-temporal response field (STRF)...

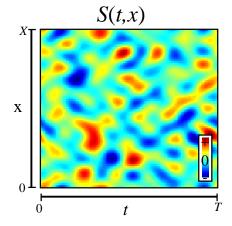
 $\begin{array}{c}
STRF(t,x) \\
x = \log f/fo \\
(octaves)
\end{array}$

...or equivalently, in the Fourier domain, by the ripple transfer function (TF).

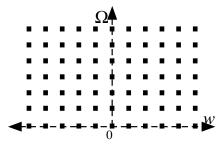


The STRF can be measured by reverse-correlating with the dynamic spectrum of a broad-band stimulus.

Dynamic Spectrum of Stimulus



Ripple Spectrum

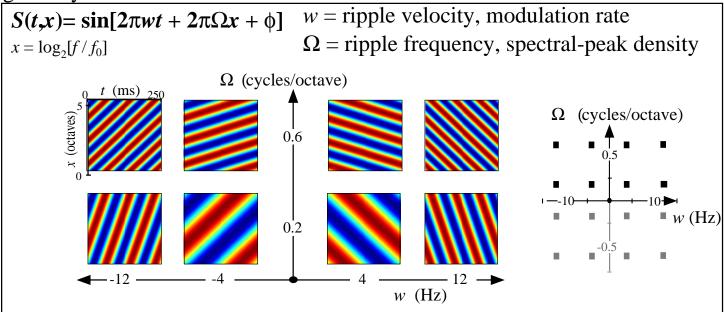


The stimuli should contain spectral-peak densities and modulation rates evenly distributed over a relevant range.



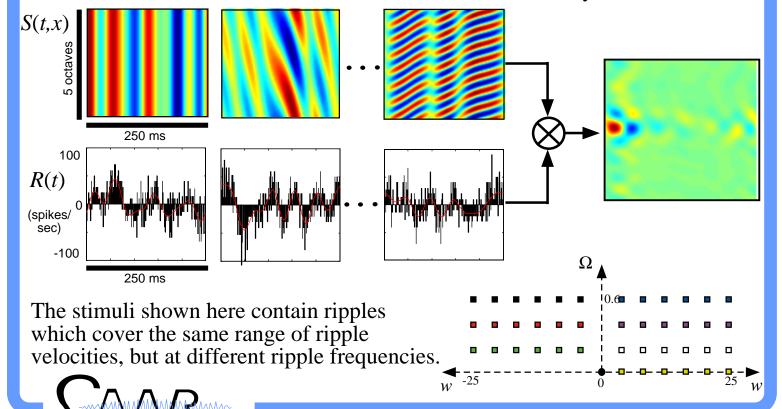
Moving Ripples

Moving ripples form our basis for the Fourier-domain description of dynamic spectra. At any time t and any frequency x, their amplitude S(t,x) is given by:



Temporally Orthogonal Ripple Combinations (TORCs)

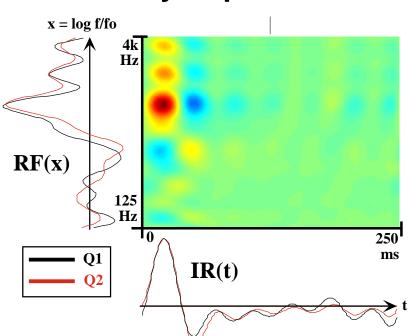
TORCs are composed only of ripples with different modulation rates. This allows us to obtain clean STRF estimates with relatively brief stimulation.



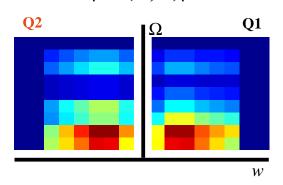
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Fully Separable STRF



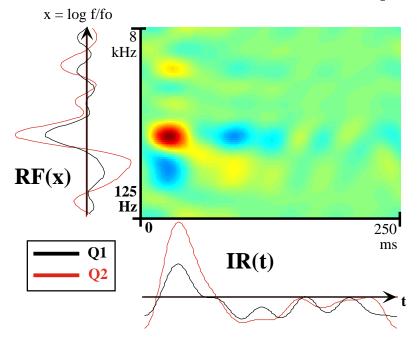
 $|\mathbf{TF}(\mathbf{w},\Omega)|$



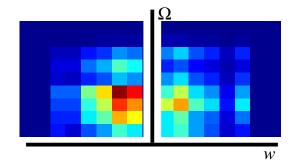
The STRF and TF are a product of a single spectral response function with a single temporal response function.

Shown above are the impulse responses (IR) and receptive fields (RF) derived from quadrant 1 (black) and quadrant 2 (red) of the transfer function by inverse Fourier transformation.

Quadrant Separable STRF



This neuron responded twice as strong to rising frequencies than it did to falling frequencies.



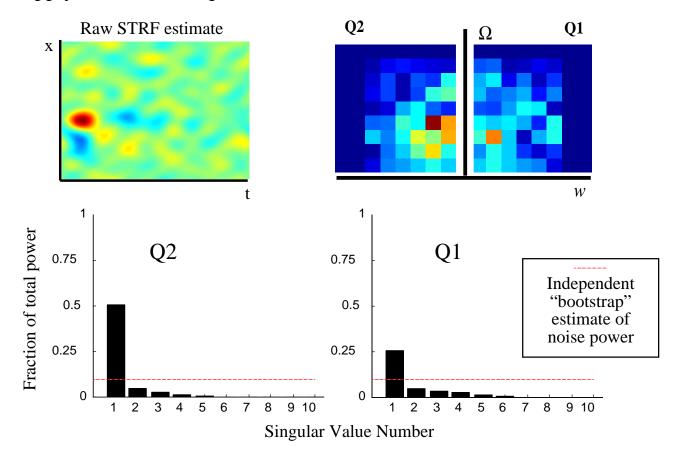
The STRF is not separable, but each quadrant of the transfer function is, i.e., there are different spectral and temporal responses for upwards and downwards frequency modulation.



Singular Value Decomposition (SVD)

for Evaluation of Separability and for Noise Reduction

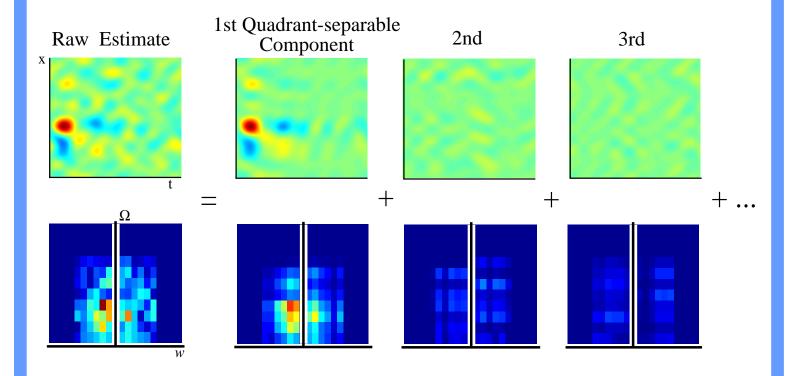
- If a quadrant of the transfer function is separable, every row is a scaled version of every other row. Such a matrix is said to have a rank of one.
- Singular Value Decomposition (SVD) can be used to estimate the rank of a matrix corrupted by noise. It decomposes the matrix into a sum of rank one (separable) matrices, ordered by their overall magnitudes. The first *k* components sum to a matrix of rank *k* which minimizes the power of the remaining components.
- We apply SVD to each quadrant of the transfer function.



• SVD naturally separates the signal and noise components of a matrix. Typically, large jumps in the singular values indicate where the separation occurs. Noise is removed by discarding the lower-magnitude components.

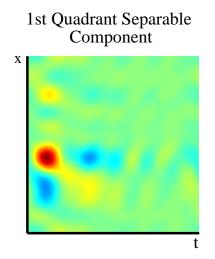


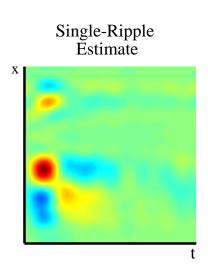
Below, STRFs corresponding to the three most significant quadrant-separable components, derived from SVD, are shown.



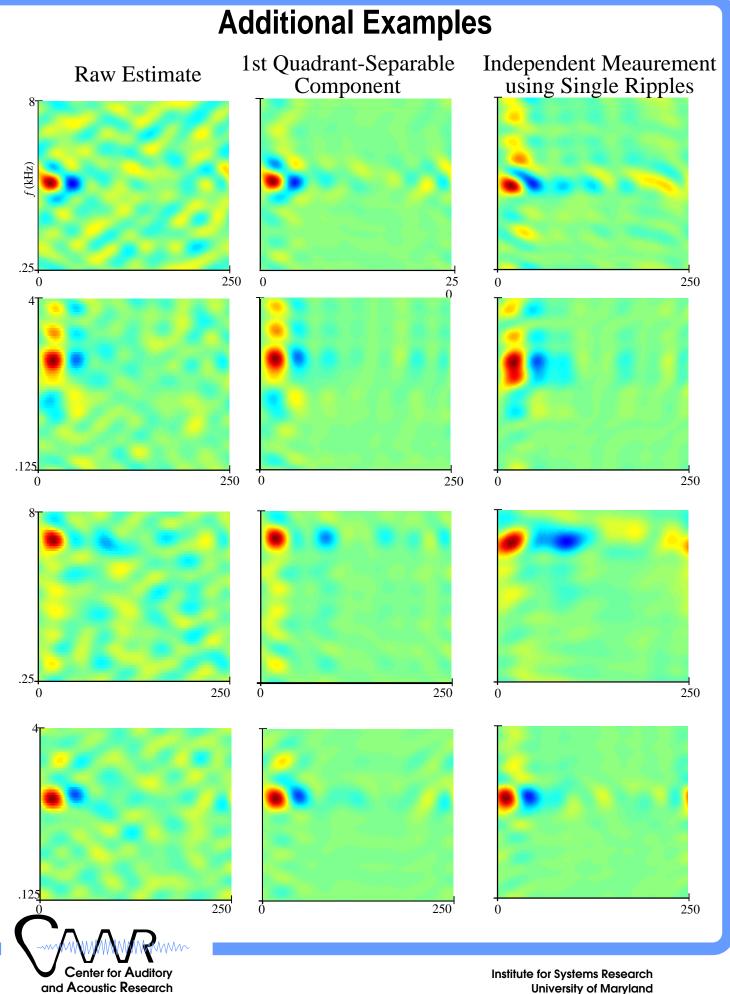
Without prior assumptions, SVD indicates that a large majority of STRFs in AI are quadrant separable.

This finding is further supported by the similarity between the first separable component and the STRF measured with a single-ripple method, for which quadrant separability had been assumed.





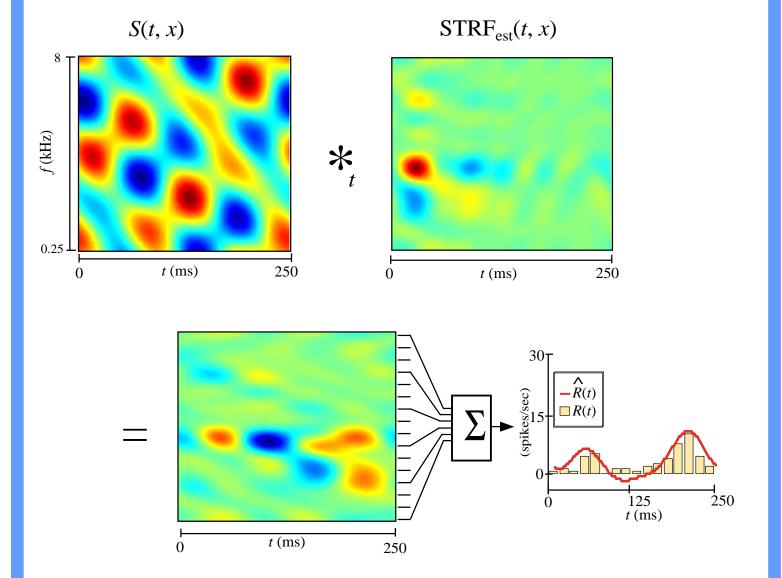




Predicting Responses from STRF

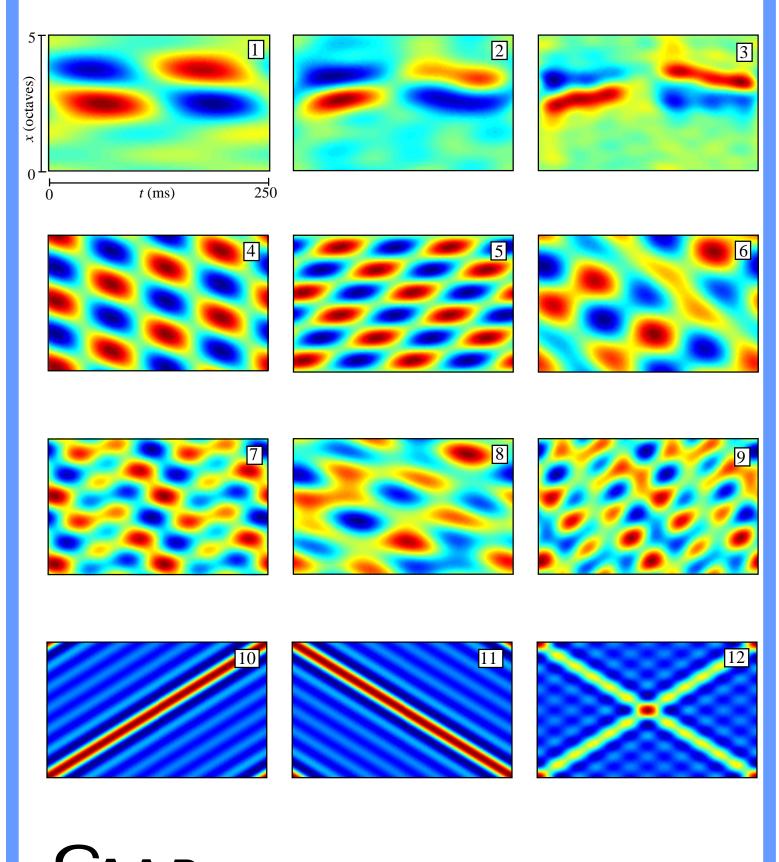
The response to an arbitrary sound is predicted by the convolution of the STRF with the stimulus' spectro-temporal envelope, plus a constant.

$$\hat{R}(t) = \frac{1}{X} \sum_{x} \{ \text{STRF}_{\text{est}}(t, x) *_{t} S(t, x) \} + \text{E}\{R(t)\}$$



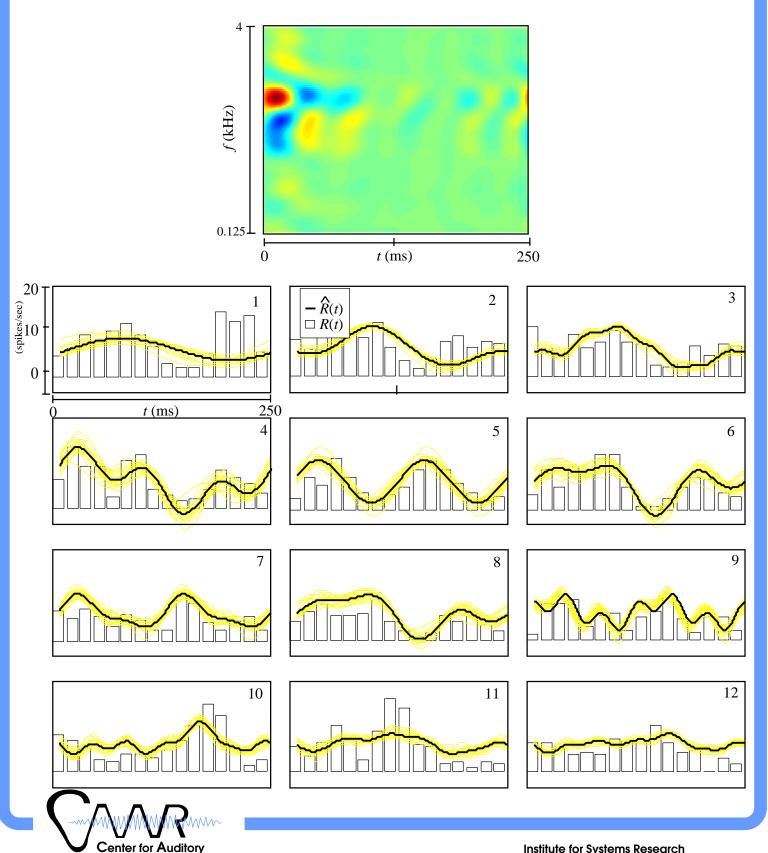


Stimuli Used for Predictions



Validation by Prediction

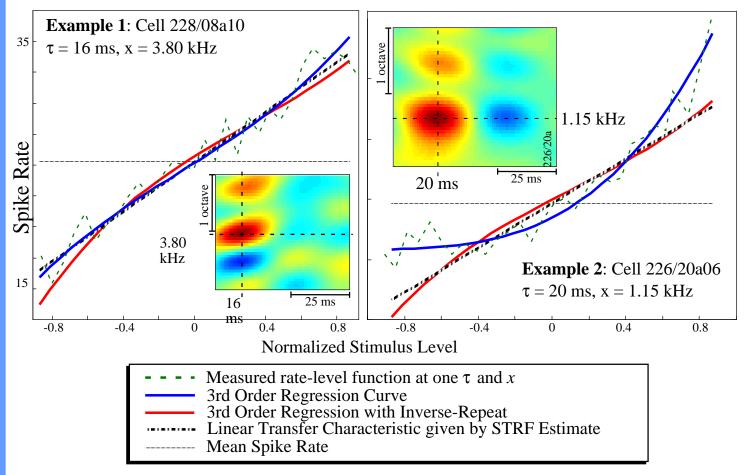
The STRF estimates often predict the magnitude and dynamics of the response well.



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Non-Linearity

- The value of the STRF at each point (τ, x) is the slope of a linear rate-level function: $R_{\tau,x}(t) = [STRF(\tau, x)] \cdot S(t-\tau, x)$.
- Polynomial rate-level curves are measured at every (τ, x) , and improve the description. These potentially non-linear functions describe the average firing rate given the stimulus level around a frequency x and at a time τ in the past.

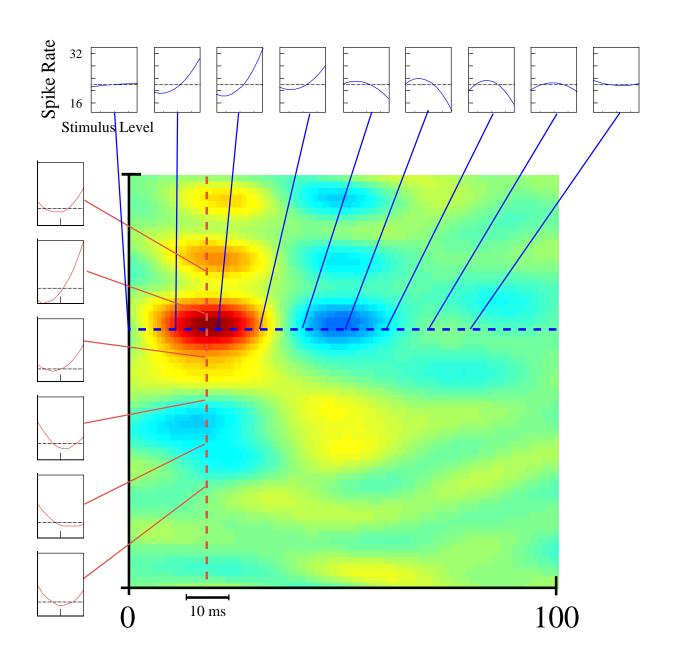


- The power series coefficients of the curves are given by the diagonals of the Volterra kernels, measured using *polynomial correlation*.
- Using cubic polynomials, we have shown that either the non-linearities are absent, or they are dominantly second order.
- Subtraction of the response to the inverted envelope gives a nearly linear polynomial fit. This would be expected, for example, from a rectifying non-linearity (i.e., purely even order).



Spectro-Temporal Rate-Level Functions

Rate-level functions change with τ and x.





Non-linearity Theory

• The STRF is the linear time-invariant filter governing the transformation from stimulus to response. Thus it can be identified with the first kernel of a Volterra series expansion of the system.

Third-order Volterra series expansion of an input S(t, x):

$$\begin{split} R(t) &= v_0 + \int d\tau \int dx \cdot v_1(\tau, x) S(t - \tau, x) \\ &+ \int d\tau_1 \int d\tau_2 \int dx_1 \int dx_2 \cdot v_2(\tau_1, \tau_2, x_1, x_2) S(t - \tau_1, x_2) S(t - \tau_2, x_2) \\ &+ \int d\tau_1 \int d\tau_2 \int d\tau_3 \int dx_1 \int dx_2 \int dx_3 \cdot v_3(\tau_1, \tau_2, \tau_3, x_1, x_2, x_3) \cdot \\ & S(t - \tau_1, x_1) S(t - \tau_2, x_2) S(t - \tau_3, x_3) \quad + \ \cdots \end{split}$$

Form of the Regression Function: (Third-order Approximation)

$$g(s;\tau,x) = E\{R(t) \mid S(t-\tau,x) = s\}$$

$$\approx a_0(\tau,x) + a_1(\tau,x) \cdot s + a_2(\tau,x) \cdot s^2 + a_3(\tau,x) \cdot s^3$$

• The regression functions describe the non-linearities within each channel, but not interactions between channels.

The true STRF is just the linear part...

$$STRF(\tau, x) \stackrel{\scriptscriptstyle \Delta}{=} a_1(\tau, x)$$

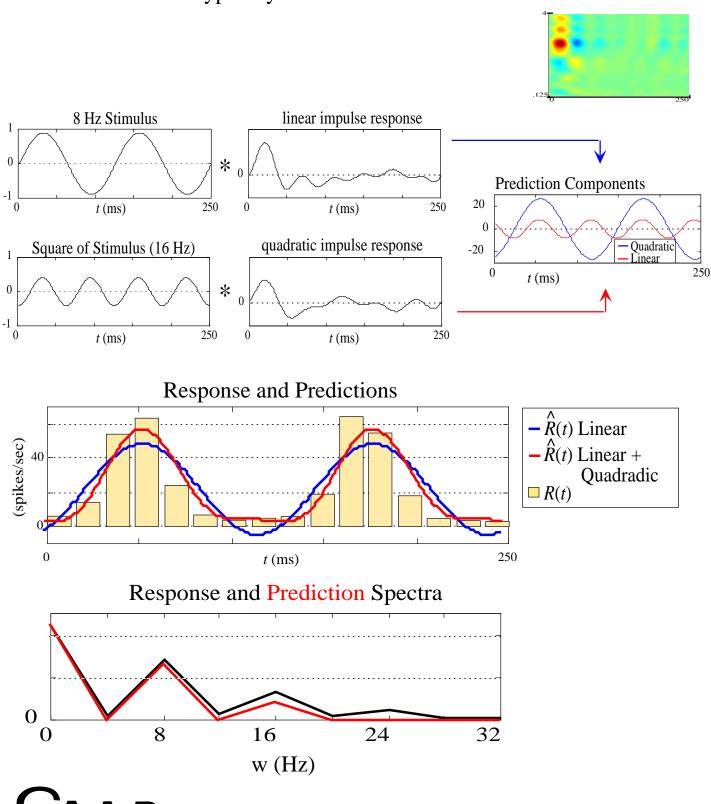
Use of the Regression Function to Predict the Response:

$$\hat{R}(t) = \int d\tau \int dx \cdot a_0(\tau, x) + \int d\tau \int dx \cdot a_1(\tau, x) S(t - \tau, x)$$
$$+ \int d\tau \int dx \cdot a_2(\tau, x) S^2(t - \tau, x) + \int d\tau \int dx \cdot a_3(\tau, x) S^3(t - \tau, x)$$



Non-Linear Prediction

• Preliminary results indicate that the non-linear predictions fit the responses more accurately than the linear predictions, although the differences between the two are typically subtle.





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Summary

- The Spectro-Temporal Response Field (**STRF**) embodies the linear component of a neuron's response to a sound's spectro-temporal envelope.
- For neurons in Primary Auditory Cortex (AI) of Ferrets, we have previously characterized the STRF and its Fourier transform: the ripple transfer function. Using single moving ripples, we found best responses to temporal modulations typically from 4 to 16 Hz, and spectral-peak densities from 0.4 to 1.6 cycles/octave.
- By reverse-correlating with temporally orthogonal ripple combinations (TORCs) enriched with these spectral and temporal qualities, we can use brief stimuli and compute clean STRF estimates "on the fly".
- Applying Singular Value Decomposition (SVD) to the measured ripple transfer functions, we found that a vast majority of STRFs in AI are quadrant separable. Moreover, we were able to isolate and discard much of the remaining noise in the STRF estimate.
- The measured STRFs are generally a good predictors of the response to broad-band sounds with arbitrary spectro-temporal structure.
- Using the same experimental paradigm, rate-level non-linearities were measured at numerous frequencies and latencies. These were mild and even-ordered, corresponding to soft-rectification and expansion, and they slightly improved response predictions.

